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Effect of mosaicity in x-ray studies of critical behavior at the nematic to smectic-A transition

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Previous studies of critical behavior at the nematic to smectic-A transition by high-resolution x-ray scattering were performed using low magnetic fields of 0.1–0.8 T. In those studies, the transverse resolution was limited by the sample mosaicity which complicated data analysis. In order to understand the effect of sample mosaicity on the measured values of critical exponents, the divergence of the smectic order correlation lengths \( \xi_{||} \) and susceptibility \( \sigma_\perp \) was studied in a magnetic field ranging from 0.25 to 5 T. The use of high (5 T) field reduced the sample mosaicity and improved the effective transverse resolution by almost two orders of magnitude. Three liquid crystals, two mixtures of 6th and 7th homologs of 4,4’-dialkylazobenzene (DnA0B) and 4-n-octyloxybiphenyl (8CB) were studied. 15 wt\%(D6.15A0B) and 40 wt\%(D6.4A0B) mixtures of D7A0B in D6A0B have a wide nematic range, while 8CB has a narrow nematic range. Analysis of the data at different fields revealed a different and proper way to apply the mosaicity correction. The Gaussian mosaicity correction was found to be temperature independent but significantly (\( \sim 3.5 \) times) smaller than the width of the sharpest \( q_z \)-scan, which has traditionally been used for mosaicity correction in all previous studies. The values of the critical exponents measured over almost four decades of reduced temperature were: \( \nu_t = 0.79 \pm 0.02 \), \( \nu_t = 0.69 \pm 0.02 \), \( \gamma = 1.46 \pm 0.04 \) for D6.15A0B; \( \nu_t = 0.79 \pm 0.02 \), \( \nu_t = 0.67 \pm 0.02 \), \( \gamma = 1.44 \pm 0.04 \) for D6.4A0B; and \( \nu_t = 0.70 \pm 0.02 \), \( \nu_t = 0.52 \pm 0.02 \), \( \gamma = 1.24 \pm 0.04 \) for 8CB. The results for the two mixtures suggest that in wide temperature range nematics, far from the tricritical point, the exponents may be material independent. No significant effects of mosaicity on the values of the coefficient \( c \) of the fourth-order term in the structure factor were observed.

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I. INTRODUCTION

Liquid crystals can be simply described as anisotropic fluids. A wide variety of phases and phase transitions are exhibited by liquid crystals. These transitions are physical realizations of a number of unique systems for which theoretical predictions have been made. One of the most interesting and most extensively studied phase transitions is the nematic to smectic-A (NA) transition. It is an example of a simple transition at which a system freezes (melts) in one dimension. However, after three decades of intense research on this topic, the NA transition still remains poorly understood. One of the serious problems is our inability to obtain reliable quantitative structural information in the close vicinity of the transition due to poor transverse resolution, which is determined by the sample mosaicity. In this paper, we report the results of a high-resolution x-ray diffraction study of the NA transition under a high (5T) magnetic field. The use of a high-field improved the effective transverse resolution by almost two orders of magnitude over previous studies and allowed us to obtain results, which were essentially free of mosaicity effects. The low-field data, analyzed without mosaicity correction, clearly demonstrated the artifact of mosaicity, which could be mistakenly attributed to crossover behavior. Using high-field mosaicity-free results as a reference revealed a different and proper way to correct the low-field data for the effects of mosaicity.

This paper has five sections. The following section gives a background of the NA transition and briefly reviews existing theoretical models and associated critical behavior. The structure factor for smectic fluctuations above the transition and a sample mosaicity are discussed in Sec. III. Sec. IV provides experimental details including the x-ray spectrometer, sample alignment, temperature control, and the methodology used. The results are presented and discussed in the last section and are followed by conclusions.

II. BACKGROUND

The nematic (N) phase has orientational but no translational order with long molecular axes aligned, on average, parallel to the unit vector \( \hat{n} \) called the director. The conventional nematic order parameter is a symmetric traceless tensor [1],

\[
Q_{ij} = \frac{1}{3} \left( n_i n_j - \frac{1}{3} \delta_{ij} \right),
\]

where \( S = \langle \frac{1}{2} \cos \theta - \frac{1}{2} \rangle \), \( \theta \) is the angle between the long molecular axis and the director, \( \langle \cdots \rangle \) means statistical averaging over all molecules and \( n_i(\alpha = x, y, z) \) are the director’s components in the laboratory frame. The magnitude \( S \) provides a measure of the degree of orientational order.

At the NA transition, the continuous translational symmetry of the nematic phase is broken, which results in condensation of a one-dimensional density wave \( \rho(z) \) along \( \hat{z} \| \hat{n} \) and formation of the smectic-A (SmA) phase. Near the transition, the density wave is often approximated by a simple sine wave. The SmA order parameter is the coefficient \( \Psi \) of the spacially dependent term in the Fourier series expansion of \( \rho(z) \) with period \( d \) equal to the smectic layer spacing [1]:
\[ \rho(z) = \rho_0 [1 + \text{Re}[\Psi e^{i\varphi}]], \]

where \( \varphi \) is the density in the nematic phase.

Therefore, \( \Psi \) can be represented as a complex number

\[ \Psi = |\Psi| e^{-i\varphi z}, \]

where \( |\Psi| \) is the amplitude of the translational order, while the phase factor \( (\varphi,\varphi_z) \) defines the position of the smectic layers.

Using a phenomenological Landau approach, de Gennes [2] wrote the following expression for the SmA free energy

\[ F_{\text{NA}} = \frac{1}{2} \int d^3r \left[ a|\Psi|^2 + b|\Psi|^4 + c_i|\nabla\Psi|^2 + c_{ij}|\nabla_i\Psi|\right], \]

where \( a, b, c_i \) are typical Landau expansion coefficients with the gradient term having different contributions from the directions parallel and perpendicular to smectic layers; \( F_{\text{NA}}(K_i) \) is the Frank elastic energy of director fluctuations [3]

\[ F_{\text{NA}}(K_i) = \frac{1}{2} \int d^3r (K_i(\nabla\cdot n) + K_2(\nabla n\times n)^2 + K_3(\nabla n\times n)^2). \]

Here \( K_i = K_{i0} + \delta K_i \), where \( K_{i0} \) are the bare values of the smectic, twist, and bend elastic constants.

There are several factors complicating the nature of the NA transition compared to the other transitions which are also described in terms of a two component complex order parameter. First of all, the coupling between the orientational and translational orders, so-called \( \Psi-S \) coupling, can change the sign of the fourth-order coefficient \( b \) in Eq. (1) and drive the NA transition first order [1]. The crossover from critical to tricritical and then to first-order behavior with decreasing nematic range was also predicted within the framework of microscopic mean-field theory by McMillan [4] and Kobayashi [5]. Another very important feature of the NA transition is the coupling between \( \Psi \) and nematic director fluctuations, or the \( \delta n\cdot\Psi \) coupling. Inclusion of this coupling described by \( c_{ij} |(\nabla_i - i\varphi_z,\delta n)|^2 \) in the SmA free energy allowed de Gennes to recognize the analogy between Eq. (1) and the Landau-Ginzburg free energy for superconductors [2]. Using this analogy Halperin, Lubensky, and Ma [6] predicted that the NA transition should always be at least weakly first order. The superconductor analogy, however, is not complete because of the broken gauge invariance [7] and the absence of true long-range order in the smectic phase due to the Landau-Peierls instability [8,9].

In spite of these complications, the NA transition was, at first, expected to be in the 3d-xy universality class [2]. However, experimental observations [10] contradicted this prediction and indicated a profound effect of the two couplings on the nature of the transition. Two major features of this transition are nonuniversal critical behavior and weak anisotropy in the critical exponents \( \nu_{ij} \) describing divergence of the correlation lengths \( \xi_{ij} \) in the directions parallel and perpendicular to smectic layer normal. Here, \( t = (T - T_{\text{NA}})/T_{\text{NA}} \) is the reduced temperature, \( T_{\text{NA}} \) is the transition temperature, and \( \xi_{ij} \) are the bare correlation lengths. Several different theoretical approaches, mostly based on the Landau-de Gennes free energy, were developed in attempts to resolve these issues. Monte Carlo studies of the lattice model [11,12] suggest that the NA transition should be in the inverted 3d-xy universality class with isotropic \( \nu_{ij} = \nu_{xx} \) critical exponents. On the other hand, the dislocation-mediated melting theory [13] predicts strongly anisotropic behavior \( \nu_{ij} = 2\nu_{xx} \), in agreement with the existence of a \( \nu_{ij} = 2\nu_{xx} \) fixed point in the anisotropic scaling theory [14]. Gauge transformation theory [15] predicts different divergences of correlation lengths measured by x-ray diffraction and light scattering and predicts that the x-ray correlation lengths should display a crossover from isotropic \( \nu_{ij} = \nu_{xx} \) to strongly anisotropic \( \nu_{ij} = 2\nu_{xx} \) divergence. Self-consistent one-loop calculations [16] predict a gradual crossover from isotropic to strongly anisotropic \( \nu_{ij} = 2\nu_{xx} \) behavior, and a broad region of weak anisotropy \( 1 < \nu_{ij} < 4/3 \) consistent with experimental observations. Finally, Garland et al. [17] showed that possible corrections-to-scaling terms also could play an important role in describing critical behavior at the NA transition. Though some aspects of experimental results agree with predictions of one or another model, none of the existing theories can explain all features of the results [10] obtained by x-ray diffraction, light scattering, and heat capacity measurements.

III. SMECTIC STRUCTURE FACTOR, SAMPLE MOSAICITY, AND DATA ANALYSIS

Our theoretical understanding of the NA transition, as described in the preceding section, is very complicated, quite controversial, and far from complete. This emphasizes the importance and need for reliable, high-precision experimental measurements, which would help one select the most appropriate theoretical approach. Experimental data in the close vicinity of the transition is of special interest, since a crossover to strongly anisotropic behavior \( \nu_{ij} = 2\nu_{xx} \) in this region is predicted by some models [15,16]. One of the sources of reliable results is high-resolution x-ray diffraction experiments, which directly probe the smectic density fluctuations in the nematic phase. However, to extract correct values of the smectic order correlation lengths and susceptibility, one has to know both, the structure factor and the experimental resolution. The latter is strongly affected by the sample mosaicity in the vicinity of the transition.

Using the harmonic approximation and neglecting the thermal fluctuations of the director, one obtains a simple Lorentzian form for the structure factor of smectic fluctuations in the nematic phase [1]. However, McMillan [18] observed a non-Lorentzian behavior of the x-ray scattering profile in the \( q_L \) direction. He also reported anisotropy of the critical exponents for the correlation lengths. These interest-
ing features were later confirmed in all x-ray studies of the critical behavior at the NA transition.

In a later study with significantly improved instrumental resolution and temperature stability, Als-Nielsen et al. [19] found that the x-ray scattering data were adequately described by the following modified Lorentzian structure factor

\[ S(q) = \frac{\sigma_o}{1 + \xi_0^2 (q - q_o)^2 + \xi_s^2 q_s^2 + \xi_l^2 q_l^2 + c \xi_s^4 q_s^4} \]  

convoluted with the instrumental resolution function. Here \( \sigma_o \) is the susceptibility of the smectic order parameter, which diverges at the transition with the critical exponent \( \gamma \), so \( \sigma_o = \sigma_o^0 t^{-\gamma} \) (\( \sigma_o^0 \) is the bare value). Als-Nielsen et al. showed that the empirical fourth-order correction term with freely adjustable parameter \( c \) improved the goodness-of-fit parameter \( \chi^2 \) for the transverse scan by 10–30 times and could be as large as 10% of the second term in \( q_s \). They suggested that the large fourth-order corrections originated from splay-mode director fluctuations and represent a precursor to the anticipated \( q_s^0 (4 + 2 n) \) line shape in the smectic phase [20]. The structure factor of Eq. (2) became well established and was used in the majority of subsequent x-ray studies of the NA transition [10].

In some studies [21,22], the x-ray data were also fit to an alternative form of the structure factor given by a Lorentzian raised to the power \( 1 - \eta_j/2 \) along the transverse direction

\[ S(q) = \frac{\sigma_o}{\xi^2 (q - q_o)^2 + (1 + \xi^2 q_s^2)^{1 - \eta_j/2}} \]  

where \( -2 < \eta_j < 0 \) is an empirical exponent that is freely adjustable in the fits. Both Eqs. (2) and (3) have four adjustable parameters with weakly temperature dependent parameters \( c \) or \( \eta_j \), reflecting a crossover in the transverse line shape, which changes from Lorentzian squared at large \( t \) to Lorentzian-like (\( c \sim 0.001, \eta_j \sim 0 \)) at small \( t \) near \( T_{NA} \) [22]. The experimental data studied in Refs. [21,22] were fit equally well with both equations and the critical exponents were found to be essentially the same for both line shapes. Moreover, Nounesis et al. [22] showed that even using Eq. (2) with fixed value \( c = 0 \) does not change the values of \( \nu_j \) and \( \gamma \). Thus, they concluded that the precise line shape used in describing a non-Lorentzian correction to the x-ray scattering profile has no significant effect on the values of the critical exponents. A similar conclusion was made by Chan et al. [23], who used a slightly different form of Eq. (3) to analyze the x-ray data.

A somewhat different approach was used by Bouwman and de Jeu [24] to account for the non-Lorentzian profile of the transverse x-ray scans. Following the assumption introduced by Als-Nielsen et al. [19], they attributed the fourth-order correction in the transverse direction to splay-mode director fluctuations. It was argued that the temperature dependent line shape results from the competition between the terms \( c_{s}(\nabla_{ij} - i q_o \delta n)^2 \) and \( K_{s}(\nabla \cdot \delta n)^2 \) in Eq. (1) for the smectic free energy. Close to \( T_{NA} \), the \( c_{s}(\nabla_{ij} - i q_o \delta n)^2 \) term should become very small (since it disappears in the smectic phase) and the line shape should be dominated by the quartic term originating from \( K_{s}(\nabla \cdot \delta n)^2 \). On the other hand, further away from \( T_{NA} \), the above assumption is not valid and the contribution of the \( c_{s}(\nabla_{ij} - i q_o \delta n)^2 \) term from \( 0.58 \) to 0.74 for \( \nu_j \), and from 1.38 to 1.64 for \( \gamma \) compared to the values obtained when \( c \) was left free. This disagrees with the results [22,23] mentioned earlier, where no significant change of the values of the critical exponents was observed.

To conclude, the empirical structure factor given by Eq. (2) has the simplest form and it quite adequately describes the experimental x-ray profiles. Currently, there is no theory which predicts this precise form of the transverse line shape. For that reason, the introduction of an independent correlation length \( \xi_j \) for \( \nu_j \) does not seem to be justified and would only further complicate the matter.

Knowing the correct form of the structure factor is necessary but not sufficient to obtain reliable values of the correlation lengths and susceptibility. The experimental resolution has to be taken into account in the data analysis to extract \( \xi_{j,2} \) and \( \sigma_o \). In the close vicinity of the transition, the resolution function becomes especially important. For example, Als-Nielsen et al. [19] first claimed that the critical exponents \( \nu_j \) and \( \nu_j \) were identical and exhibited a crossover from 3d-XY to mean-field values on approaching \( T_{NA} \). However, these conclusions did not remain valid, when the correct form (Lorentzian) of the longitudinal resolution function was used to reanalyze the data.

The effective resolution function in an x-ray scattering experiment near the NA transition depends on two factors. The first comes from the instrumental resolution of the x-ray
spectrum and the second from the imperfect alignment of the sample. The layers in different (fluctuating) correlated volumes (domains) of the nematic phase are not perfectly parallel to each other but have a finite distribution, which is referred to as mosaic distribution or the mosaicity.

In x-ray experiments, longitudinal ($q_l$) and transverse ($q_{\perp}$) scans are performed above the NA transition. During a $q_{\perp}$-scan, both the sample and the detector are rotated simultaneously, so the detector measures scattering from the set of smectic domains which satisfy the Bragg condition. Since the width of the $q_{\perp}$-scan is proportional to $\xi_{\perp}^{-1}$ [see Eq. (2)], it decreases as $T$ approaches $T_{NA}$ until it reaches the value of the longitudinal instrumental resolution, $\Delta q_l$. On the other hand, the sample is rotated during a $q_{\perp}$-scan to affect lateral changes in $q_{\perp}$. Far from $T_{NA}$, where the mosaicity effect is small, the width of the $q_{\perp}$-scans is roughly proportional to $\xi_{\perp}^{-1}$ [see Eq. (2)]. However, close to $T_{NA}$ the mosaicity becomes significant and the width of $q_{\perp}$-scans saturates at the mosaicity limit, $\Delta q_{\perp}$, rather than at the instrumental transverse resolution $\Delta q_{\perp}$. Since typical high-resolution x-ray spectrometers have $\Delta q_{\perp} \approx 10^{-5}$ Å$^{-1}$, the effective transverse resolution in the scattering plane is always determined by the sample mosaicity. Thus, the mosaicity sets the lower boundary on the reduced temperature below which reliable values of $\xi_{\perp}$ and $\sigma_{\perp}$ can no longer be obtained.

All previous x-ray studies [10] of critical behavior near the NA transition have been performed in a magnetic field range $B \approx 0.1$--0.8 T with the reported values of the mosaicity full width at half maximum (FWHM) ($\Delta q_M$) varying from $1.7^\circ$ ($6 \times 10^{-3}$ Å$^{-1}$) [25] to $0.1^\circ$ ($4 \times 10^{-4}$ Å$^{-1}$) [26]. These values are substantially larger than the instrumental transverse resolution $\Delta q_{\perp} \approx 10^{-5}$ Å$^{-1}$. In the first study [25], low magnetic fields $B = 0.08$ T and $B = 0.18$ T were used to align the samples. The mosaic width was estimated from the limiting transverse line width as $t \to 0$ and was assumed to be temperature independent for $t > 0$. Davidov et al. [25] mentioned that the last assumption was likely a poor approximation far from $T_{NA}$. The mosaicity profile was modeled by a Gaussian of the corresponding width and included in the data analysis to deconvolve the structure factor. The correction was found to be negligible over the complete temperature range ($5 \times 10^{-5} < t < 1 \times 10^{-3}$) for the 0.18 T experiment. However, it was substantial for $t < 2 \times 10^{-4}$ for the 0.08 T measurements.

Mosaicity was also taken into account by Chan et al. [23] who used a 0.45 T aligning field. They argued that the narrowest observed mosaicity ($0.4^\circ \approx 9 \times 10^{-4}$ Å$^{-1}$ FWHM) remains unchanged in the nematic phase. This argument was based on the assumption that the precise sample alignment or at or above the transition temperature, though unknown, should depend only on the uniformity of the magnetic field. The Gaussian mosaicity correction used in Ref. [23] affected the points where $\xi_{\perp}^{-1}$ was less than or comparable to the mosaicity width. However, the corrected results did not improve the power-law fits and, in fact, made them slightly worse. In addition, when the transition temperature was allowed to vary, the critical exponents became identical to the values obtained without mosaicity corrections. From these findings Chan et al. concluded that corrections for mosaicity were smaller than the precision of their experiments.

The insignificance of mosaicity corrections was also reported in several other papers. Kortan et al. [26] observed a mosaicity range from $0.1^\circ$ to $0.4^\circ$ in a 0.4 T field. They conclude that the correction for mosaicity did not alter the results when the mosaicity was less than $0.001q_o$ ($q_o = 0.0206$ Å$^{-1}$) and only affected the points closest to $T_{NA}$. Ocko et al. [21] performed experiments with various aligning field strengths (0.6--0.8 T) for some of the samples. They concluded that the critical behavior in the nematic phase did not depend on the field strength, although the mosaicity in the smectic phase did. Therefore, they assumed that the effects of mosaicity in the nematic phase can be neglected. Chen et al. [27] reported the mosaicity widths $2.24^\circ$ ($9.2 \times 10^{-3}$ Å$^{-1}$), $0.72^\circ$ ($3.0 \times 10^{-3}$ Å$^{-1}$) and $0.26^\circ$ ($1.1 \times 10^{-3}$ Å$^{-1}$) for their three samples studied in a 0.25 T field. They applied a Gaussian mosaicity correction for the $0.72^\circ$ mosaicity sample. The exponents obtained after mosaicity correction were essentially identical to those for the sharpest mosaicity ($0.26^\circ$) but without using mosaicity correction.

Unlike the results discussed above, Bouwman and de Jeu [24] indicated that correction for the mosaicity has a strong influence on the extracted parameters. They studied the NA transition for two different materials in a 0.4 T field and obtained the mosaicity values of $0.4^\circ$ ($1.5 \times 10^{-3}$ Å$^{-1}$) for one and $0.56^\circ$ ($2.0 \times 10^{-3}$ Å$^{-1}$) for a different sample. Since the experimental mosaicity profiles were well described by a Lorentzian, Bouwman, and de Jeu used a Lorentzian rather than Gaussian mosaicity correction. The corrected values of the critical exponents for the material with the wider mosaicity of $0.56^\circ$ increased from 0.82 to 0.91 for $\nu_l$ from 0.58 to 0.72 for $\nu_{\perp}$ and from 1.38 to 1.62 for $\gamma$. The corrections for the material with narrower mosaicity ($0.4^\circ$) affected only the values of $\nu_{\perp}$ and $\gamma$. Concerned with the large effects of mosaicity corrections, Bouwman and de Jeu questioned the validity of the assumption that the sharpest mosaicity observed remains unchanged in the nematic phase. They argued that the mosaicities in the two phases have different origins. The mosaicity in the smectic phase is caused by effects of the boundaries penetrating into the bulk of the sample. On the other hand, the penetration length for defects in the nematic phase is of the order of microns and the mosaicity in the nematic phase should only depend on temperature gradients in the sample. Using these arguments Bouwman and de Jeu concluded that the measured mosaicity is an overestimation.

So far, we have only discussed the consequences of the mosaicity correction on the values of the critical exponents. A different effect of the mosaicity on the line shape of transverse x-ray scans was pointed out by Dasgupta [12]. During time evolution of his Monte Carlo simulation of the NA transition, parts of the system sometimes fluctuate into the vicinity of one of the ground states corresponding to small global
rotations of the system. These fluctuations cause the simulated correlation function \( g(q_z) \) to fall off faster than a Lorentzian for relatively large values of \( q_z \) while \( g(q_i) \) remains unaffected. Dasgupta showed that the imposition of constraints, which suppress these fluctuations, brings \( g(q_z) \) closer to the Lorentzian form and also causes an increase in \( \xi_z \). He suggested that similar effects in real systems may be produced by the sample mosaicity. He argued that the effect of averaging over a sample with finite mosaic distribution would essentially be the same as that of time averaging during evolution where parts of the system undergo small uniform rotations. He also claimed that convoluting a Lorentzian with a Gaussian mosaicity function produces the lineshape in experiments. Based on this analysis, it was suggested that a careful experimental study of the effects of mosaicity should provide important insight into the puzzling critical behavior at the NA transition.

IV. EXPERIMENTAL DETAILS

In our study, we used two mixtures of the sixth and seventh members of the 4,4'-dialkylazoxybenzene (DnAOB) homologous series, as well as 4-n-octylcyanobiphenyl (8CB). Their chemical formulas are shown in Fig. 1. The three members of the DnAOB series \((n=6,7,8)\), which are also referred to as D6AOB, D7AOB, and D8AOB exhibit a simple isotropic-N-SmA phase sequence. The sixth homolog has the widest nematic range with \( T_{NA}/T_{NI} = 0.88 \). Light scattering studies \([28]\) of the twist elastic constant provide evidence that the NA transition in D6AOB is continuous to within at least 0.1 mK. The optical birefringence \([29,30]\), diamagnetic susceptibility \([31]\), and x-ray measurements \([27]\) on D6AOB and D6AOB + D7AOB mixtures were also consistent with second-order behavior. However, the SmA phase in pure D6AOB is monotropic and addition of \( \geq 10\% \) wt D7AOB is necessary to ensure the SmA phase stability required for x-ray measurements. We prepared 15 wt% (D6.15AOB) and 40 wt% (D6.4AOB) mixtures of D7AOB in D6AOB with \( T_{NA}/T_{NI} = 0.89 \) and 0.91, respectively. Here, D6.xAOB represents a mixture of D6AOB and D7AOB, with \( x \) being the weight fraction of D7AOB. The results of a previous study \([31]\) indicated that the NA transition becomes first order for approximately 46% concentration of D8AOB in D7AOB. Thus, both of our mixtures had the NA transitions well removed from the tricritical point and were good candidates for critical behavior studies. The NA transition in 8CB (\( T_{NA}/T_{NI} = 0.98 \)) is believed to be very close to the tricritical point \([21,32]\) and perhaps weakly first order \([33–36]\). It was studied to compare the results of high-field measurements with previous results obtained by x-ray \([21,25]\) and light scattering \([37]\). The values of \( T_{NA} \) for all three samples were in the convenient \( \sim 20–30 \, ^\circ\text{C} \) range.

The x-ray scattering experiments were done using a 12 kW Rigaku RU-200 rotating anode generator, a two-circle Huber goniometer with a pair of Si (111) single crystals as monochromator and analyzer, and a 5 T superconducting magnet. A schematic diagram is presented in Fig. 2. \( K\alpha \) lines emitted by the target (Cu or Mo) Bragg diffracted from the monochromator. Several \( xy \) slits were used to collimate the beam and define its crosssection. The slit \( S_3 \) before the magnet was also used to block the Cu \( K\alpha_2 \) line. This resulted in essential loss of intensity (\( \sim 75\% \) due to partial overlapping of the two lines) but simplified the data analysis. Unfortunately, we could not block the Mo \( K\alpha_2 \) line as it was spatially too close to \( K\alpha_1 \) line and the loss of intensity was unacceptable. The monochromatic and well collimated x-ray beam impinged on the sample placed inside the oven inserted in the superconducting magnet. The magnet had a special split-coil design, which features horizontal field and two orthogonal horizontal bores. The x-ray beam passed through one of the bores, while the field was parallel to the axis of the second bore. The magnet was mounted on the \( \theta \) circle of the two-circle Huber goniometer. The angles \( \theta \) and \( 2\theta \) were changed with a precision of 0.00025°. X-ray photons scattered from the sample were Bragg reflected from the analyzer and counted with a Na(Tl)I scintillation detector. To avoid effects of any power fluctuations in the x-ray source, the intensity of the scattered beam was measured against the incident monochromatic beam flux.

The longitudinal resolution of the spectrometer was \( \Delta q_z \approx 2 \times 10^{-4} \, \AA^{-1} \) FWHM. For the Cu target, the longitudinal resolution function has a single peak corresponding to the Cu \( K\alpha_1 \) line, which is well described by a sum of three Lorentzians \([21]\) convoluted with the energy broadening Lorentz-
ian. However, for the Mo target, both lines of the Mo $K\alpha_{1,2}$ doublet can be resolved because of dispersion at nonzero angles, and the longitudinal resolution was modeled by a sum of six Lorentzians. The transverse in-plane resolution is smaller by a factor of $\sin \theta (\sim 40$ times for $\theta \sim 1.5^\circ$) than the longitudinal resolution and can be approximated by a delta function. However, in practice, the resolution in the transverse direction is limited by the sample mosaicity rather than the instrumental resolution. The effective transverse resolution and, thus, the sample mosaicity, was measured and then used in the data analysis. The out-of-plane instrumental resolution can be modeled by the convolution of two square waves, which produces a trapezoidal function, usually approximated by a Gaussian [9,24]. Our calculations gave the Gaussian width $\sigma_z = 4 \times 10^{-2}$ Å$^{-1}$ for the Cu $K\alpha_1$ line and $\sigma_z = 8 \times 10^{-2}$ Å$^{-1}$ for the Mo $K\alpha$ doublet. In principle, the vertical resolution may also be affected by the sample mosaicity, which should have similar shape in all directions perpendicular to the aligning field. However, the mosaicity width is almost always negligible compared to the instrumental values of $\sigma_z$.

The sample, typically 1 mm thick and 6 mm in diameter, was sealed between two thin (38 µm) Mylar sheets spaced with a Teflon O-ring. The Mylar windows and the O-ring were held between two aluminum plates, thus sealing the sample. The sample cell was placed inside a two-stage oven and the oven was inserted horizontally in the superconducting magnet. The sample was positioned exactly in the center of the magnet.

The sample was first heated to the isotropic phase and then cooled down slowly in the presence of a predetermined magnetic field to a temperature about 3 K above $T_{NA}$. In order to make measurements in different fields, the magnetic field was first lowered to 0 T, the sample temperature was then raised to the isotropic phase, and then the magnet charged to a new field. This precaution was necessary to avoid any possible memory (remnant alignment) effects in the sample.

The two-stage cylindrical oven, 5.5" long and 1.9" in diameter was specially designed to fit inside the 2" magnet bore. The inner stage had beryllium windows and the outer stage openings were covered with thin Mylar films. Both stages were controlled independently by home-made temperature controllers. The temperature of the outer stage was set about 1° below $T_{NA}$, while the inner stage temperature was monitored and controlled by the computer during the experiment. The temperature stability was found to be $\leq \pm 1 mK$ over a long term (24 h) and $\leq \pm 0.5 mK$ over a short term (1 h).

The D6.15AOB sample had a phase transition temperature $\sim 20 ^\circ C$, a few degrees below the room temperature. In order to control the temperature of this sample, two cooling coils made of thin copper tubing were inserted inside the magnet bore, one on each side of the oven. A refrigerated circulating bath was used to flow cold liquid at a constant temperature through the coils in order to lower the ambient temperature outside the oven to $\sim 15 ^\circ C$.

Very near $T_{NA}$, a sample temperature gradient should result in "apparent" coexistence of the $N$ and SmA phases. Very near $T_{NA}$, a sample temperature gradient should result in "apparent" coexistence of the $N$ and SmA phases. The appearance indicates the coexistence of the $N$ and SmA phases, i.e., the presence of temperature gradients.

The scattering from the $N$ phase and the quasi-Bragg scattering from the SmA phase give different contributions to $q_{\perp}$-scans. As a result, in the presence of large enough temperature gradient the $q_{\perp}$-scans should display a sharp smectic spike on top of a relatively broad nematic peak. If the gradients are larger than the temperature stability very near $T_{NA}$, $q_{\perp}$-scans for at least one temperature point should exhibit this "spikey" shape. The signature of such coexistence behavior was, indeed, observed in the preliminary studies done with a one-stage oven without Be windows (see Fig. 3). However, it has not been seen with the two-stage oven described above. Thus, we concluded that temperature gradients in our experiments were less than 0.1 mK/mm.

Small drift in the phase transition temperature was observed in all three samples and taken into account in the data analysis. The initial drift in the D6.15AOB sample was about 5 mK/day but stabilized at 0.5 mK/day for subsequent scans of this sample. The D6.4AOB sample had a $T_{NA}$ drift of 3 mK/day for a large part of the measurements. Later it reduced to the same small rate $\sim 0.5 mK/day$. Finally, the 8CB sample had the drift rate of 2 mK/day. This slight drift in transition temperatures could be related to sample decomposition.

V. RESULTS AND DISCUSSION

By charging the superconducting magnet at different currents we could vary the applied magnetic field over a large

![Graph showing transverse in-plane scans for 8CB very near $T_{NA}$](image)
0.25–5 T range and study the field dependence of the sample mosaicity. Figure 4 shows the sharpest $q_{||}$-scans at different fields for the D6.15AOB sample. These were recorded at the experimental temperature closest to $T_{NA}$ and normalized for comparison. Since $\xi_\perp \rightarrow \infty$ at $T_{NA}$ and the correlation function $S(q_{||})$ [see Eq. (2)] becomes infinitely sharp, these scans represent the effective transverse resolution at different field strengths and their width $\Delta q_M(B)$ is closely related to the mosaicity width at the transition. It is important to note that the 5 T scan is several times sharper than the longitudinal resolution $\Delta q_{||}$ and is essentially limited by the instrumental transverse resolution $[\Delta q_M(5 T) \sim \Delta q_{||}]$. The 5 T scan was better fit by a triple Lorentzians just as the resolution limited $q_{||}$-scan, while all other scans were reasonably well fit by a single Lorentzian. The use of a 5 T field improved the effective (mosaicity limited) transverse resolution by 80 times compared to a 0.1 T field used in Ref. [25] and by 60 times compared to a 0.25 T field used in Ref. [27]. Thus, the effects of sample mosaicity on the 5 T data were found to be negligible. However, the sample mosaicity became more important in low-field experiments.

To make this argument quantitatively, we found it reasonable to define the reduced temperature $t_M$, at which the effects of mosaicity become significant. As we have discussed, the scattering from smectic fluctuations in the nematic phase is well described by the structure factor $S(q)$ given by Eq. (2). The mosaicity effects have to be considered when the width of $S(q_{||})$ (roughly proportional to $\xi_\perp^{-1}$) is comparable to $\Delta q_M$. Since $\xi_\perp$ is known to diverge as $\xi_\perp^2 t^{-\nu_\perp}$, we can estimate $t_M$ from the condition $\xi_\perp/(\Delta q_M)^{-1}$, which gives $t_M^{-1} = (\xi_\perp^{-1} \Delta q_M)^{1/\nu_\perp}$. Thus, the mosaicity corrections become important and should be taken into account if $t \leq t_M$ is accessed during an x-ray experiment. On the other hand, they are expected to be insignificant for data points in the region $t > t_M$. We have to point out that for the typical value $v_\perp \sim 0.6$ the estimate gives $t_M(5 T)/t_M(0.25 T) \sim [(\Delta q_M(5 T)/\Delta q_M(0.25 T))]^{1/\nu_\perp}$.

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Therefore, a 5 T field allows one to access three more decades of reduced temperature than a 0.25 T field. However, there are two more characteristic reduced temperatures in experiments. The first is the temperature stability $\Delta T$ of the oven ($t_1 \sim \Delta T/\Theta_{DA}$), while the second is related to the longitudinal instrumental resolution $\Delta q_{||}$ and can be estimated as $t_1^{-1} = (\xi_\perp^2 \Delta q_{||})^{1/\nu_\perp}$. The largest value out of $t_1$, $t_M$ and $t_1$ sets the lower boundary on the range of reduced temperature, where reliable data can be obtained.

The critical divergence of the correlation lengths and susceptibility in the D6.15AOB sample was studied under three different strengths of magnetic field (5 T, 0.5 T, and 0.25 T). The longitudinal $q_{||}$-scans and in-plane transverse $q_{\perp}$-scans were performed over ~3.5 decades of reduced temperature. To obtain reasonably good statistics the counting time varied from ~6 h per scan far from $T_{NA}$ to ~30 min per scan in the close vicinity of $T_{NA}$ ($t \sim 10^{-5}$). The representatives in the different regions of $t$ for the 5 T experiment are shown in Fig. 5. The data were first analyzed without mosaicity correction by fitting both $q_{||}$- and $q_{\perp}$-scans simultaneously to the convolution of the structure factor given by Eq. (2) with the instrumental resolution function. Data analysis was carried out with the commercial software packages C-Plot [38] and Mathematica [39], which both produced almost identical results. The fitting parameters were the correlation lengths $\xi_{||}$, the susceptibility $\sigma_0$, the fourth-order coefficient $c$, the smectic wave vector $q_0$ (nearly temperature independent in our studies), and a constant background term. Fixing the values of $q_{||}$ at the experimental value did not influence the fitting results. Using this procedure for every temperature, we obtained the temperature dependences of $\xi_{||}$ and $\sigma_0$ for different magnetic fields. The phase transition temperature was located with 1 mK precision by monitoring the width and the shape of the $q_{||}$-scans. Upon entering the SmA phase the alignment imposed by the magnetic field is distorted by thermal expansion and boundary effects penetrating into the bulk. As a result, the $q_{||}$-scans become slightly wider and often asymmetric immediately below $T_{NA}$. Thus, the transition was identified by the sharpest $q_{||}$ scan, while the appearance of the asymmetric shape (see Fig. 6) provided extra evidence for the system entering the SmA phase.

Figure 7 shows the log-log plots of the dimensionless quantities $q_0^2 \xi_{||}(t)$ and $\sigma_0(t)$. Here, the reduced temperature $t$ was calculated using the experimental value of $T_{NA}$. The 5 T data fall on straight lines indicating simple power-law divergences, i.e., $\sigma_0 = \sigma_0^* t^{-\gamma_0}$, $\xi_{||} = \xi_{||}^* t^{-\nu_{||}}$, and $\xi_\perp = \xi_\perp^* t^{-\nu_\perp}$. As expected, no mosaicity effects were seen in the 5 T data, which are in the $t > t_M^{-1}$ regime. These data are free from the effects of sample mosaicity and represent the
true divergence of the correlation lengths and the susceptibility. On the contrary, the low-field data at 0.5 T and 0.25 T clearly indicate the signature of mosaicity. Far from the transition, in the low-field regime, the mosaicity effects are insignificant and the values of $\xi_{\perp}$, $\xi_{\parallel}$, and $\sigma_0$ for high and low fields are the same. However, as one approaches the transition and enters the $t < t_M$ regime around $t \approx 10^{-5}$, the effects of mosaicity become important and cause the bending of the curves $\xi_{\parallel}(t)$ and $\sigma_0(t)$ away from the 5 T data. Similar behavior was also observed in weekly first-order systems. However, our previous arguments and the 5 T results completely rule out this possibility for D6.15AOB. It is important to note that this bending is a pure artifact of sample mosaicity and has nothing to do with any type of crossover behavior.

The low-field data must be properly corrected for the mosaicity in order to “unbend” the curves and restore the true values of $\xi_{\parallel}(t)$ and $\sigma_0(t)$. One must be cautious against fitting the low-field data to straight lines and treating $T_{NA}$ as a fitting parameter. This can artificially yield single power-law fits by forcing the best fit value of $T_{NA}^{fit}$ to be significantly lower than the experimental value $T_{NA}^{expt}$. Clearly, fitting the mosaicity-affected results to straight lines with floating $T_{NA}$ produces wrong transition temperatures. This causes the data points to shift to larger values of reduced temperature making it impossible to approach as close to the transition as allowed by the temperature stability (see Fig. 8). This seems to be the case in the majority of previous x-ray studies, where the data points were shown only for the range $t \approx 10^{-5}$ with the reported temperature stability of 1 mK (or smallest $t \approx 3 \times 10^{-6}$).

To correct the D6.15AOB data for the effects of the sample mosaicity, the smectic structure factor $S(\mathbf{q})$ was convoluted with the instrumental resolution function and the sample mosaicity modeled by a Gaussian. The Gaussian mosaicity width $\sigma_M$ was first set to the width of the sharpest $q_{\perp}$-scans (i.e., $\sigma_M = \Delta q_M$) as it has been previously done [25,23,27]. The corrections for the 5 T data were found to be negligible, in full agreement with our expectations. On the other hand, the mosaicity correction with $\sigma_M = \Delta q_M$ applied to the low field data resulted in unexpectedly large changes in the values of the correlation lengths and the susceptibility. Not only the fits to the data very near $T_{NA}$ produced extremely large values of $\xi_{\parallel}$ and $\sigma_0$ with $\approx 100\%$ uncertainties, but also the rest of the data were found to have unrealistically larger values of $\xi_{\parallel}$ and $\sigma_0$ than the corresponding...
5 T values (see Fig. 9). These calculations indicate that fixing the mosaicity width $\sigma_M$ from the sharpest $q_\perp$-scan is not a proper correction for the mosaicity. It is interesting to note very large effects of the mosaicity correction previously reported by Davidov et al. [25]. Bouwman and de Jeu [24] also obtained very large corrections for $\xi_L$ and $\sigma_o$, which resulted in $\sim 10\%$ increase in the values of $\nu_\perp$ and $\gamma$. In addition, Chan et al. [23] mentioned that the mosaicity correction did not improve the power-law fits, but made them worse. Clearly, previous researchers had encountered similar anomalies in data analysis.

Since the traditional $\sigma_M = \Delta q_M$ correction failed, we tried a different approach. We chose one data point in the vicinity of the transition and varied $\sigma_M$ until the corrected values of $\xi_L$ and $\sigma_o$ became close to the corresponding values obtained with 5 T field. Once such a value of $\sigma_M$ had been found, it was used to correct the rest of the data. Using this procedure, we obtained an excellent agreement (see Fig. 10) between the corrected low-field data and the mosaicity free 5 T data. In addition, the average values of $T_{NA}^{\text{ext}}$ obtained with this method were less than 0.5 mK away from $T_{NA}^{\text{ext}}$ giving us another half decade of useful data. However, the value of $\sigma_M$ necessary to obtain such a good agreement was roughly 3.5 times smaller than measured $\Delta q_M$ for both sets of the low-field (0.5 T and 0.25 T) data. Thus, our results support one of the previously used assumptions that the mosaicity width does not vary with temperature in the $N$ phase, but reveal that the actual mosaicity width is significantly smaller than the width of the sharpest $q_\perp$-scan $\Delta q_M$. This is consistent with the Bouwman and de Jeu [24] assumption that the sharpest $q_\perp$-scan overestimates the mosaicity.

The values of the critical exponents obtained for the D6.15AOB sample were $\gamma = 1.46 \pm 0.04$, $\nu_\perp = 0.79 \pm 0.02$, $\nu_\parallel = 0.69 \pm 0.02$. The temperature dependences of $\xi_L$ and $\sigma_o$ are described well by single power-laws over $\sim 3.5$ decades of reduced temperature. Reliable values of $\xi_L$ far away from the transition could not be obtained, because in this region the $q_\perp$-scans required a wide range of scattering angles which were not accessible in this magnet because of the magnet bore dimensions. Though the truncated $q_\perp$-scans, fitted simultaneously with $q_\parallel$-scans, produced larger uncertainties in the values of $\xi_L$, they were very useful and helped to obtain correct values of $\xi_L$ and $\sigma_o$. The reported errors in the exponents were estimated from temperature range shrinking. The values of $\nu_\parallel$ and $\nu_\perp$ appear to be slightly larger than but within the range of error bars of the values $\nu_\parallel = 0.75 \pm 0.05$ and $\nu_\perp = 0.65 \pm 0.05$ previously reported for a slightly different concentration D6.1AOB [27]. This small increase can be attributed to the different mosaicity correction. It is not reasonable to expect a large manifestation of mosaicity, since a small number of mosaicity-affected data points near $T_{NA}$ can not significantly change the values of the critical exponents.

The critical divergence of $\xi_L$ and $\sigma_o$ in the D6.4AOB sample was also studied under different fields (0.5, 0.75, and 0.5 T). These studies were done using the Mo target to access a wider $q_\perp$ range. Peaks corresponding to the two,
$K\alpha_1$ and $K\alpha_2$, lines were resolved in the $q_{\perp}$-scans close to the transition. The fits were obtained the same way as for the D6.15AOB sample but included one extra adjustable parameter for the intensity ratio of the two $K\alpha$ lines, while the separation between the two peaks ($\Delta q_M$) was calculated. The results obtained without mosaicity correction are shown in Fig. 11, where the average $T_{N_A}$ was only 0.4 mK away from $T_{N_A}^{exp}$. Since the Mo target gave us access to a wider $q_{\perp}$-range, the values of $\xi_{||\perp}$ and $\sigma_\varphi$ were not truncated at large $t$ as in the case of the D6.15AOB sample. Unfortunately, the Mo target developed a pin-hole leak before we could perform scans at 0.25 T field, where the effects of mosaicity are most profound. The results for the D6.4AOB sample at relatively higher fields were not noticeably affected by the mosaicity. This is consistent with the fact that the effective transverse resolution at 0.5 T for D6.4AOB $\Delta q_M=6.0\times10^{-4}$ Å$^{-1}$ was almost half of the value $\Delta q_M=1.1\times10^{-3}$ Å$^{-1}$ obtained for D6.15AOB at the same field. Since the mosaicity effect at 0.5 T for D6.15AOB was already marginal and the value of $t_M [\approx (\Delta q_M)^{1/2}]$ even smaller for D6.4AOB, the mosaicity affected regime $t\approx t_M$ was not accessed in our experiments for D6.4AOB. The temperature dependences of $\xi_{||\perp}$ and $\sigma_\varphi$ obtained over almost four decades of reduced temperature ($t$ for any x-ray study) are fit very well by single power-laws suggesting the absence of any crossover behavior as predicted by theories. The values of the critical exponents obtained for high (5 T) and low (0.5 T) fields are

$\Delta q_{\varphi}=0.232$ Å$^{-1}$. The solid lines are the single power-law fits with the exponents given in the text.
the same. This indicates that there is no noticeable effect on
the critical behavior up to a field of 5 T. Finally, the values of
the critical exponents, $n = 0.79 \pm 0.02; n' = 0.67 \pm 0.02; \text{ and } g = 1.44 \pm 0.04$ for D6.4AOB are the same as those for
D6.15AOB within experimental errors. It appears that, far
from the tricritical point, the critical exponents are the same
for the two mixtures studied, and perhaps in general.

We have to admit here that critical behavior studies of the
DnAOB mixtures are not complete without experimental
data on heat capacity. Such data would help to understand
the importance of corrections-to-scaling terms in describing
the NA transition. This was pointed out by Garland
et al. [17], who used both high-resolution x-ray diffraction and
heat capacity experiments to study several SmA materials.
They showed that critical behavior of the correlation volume
and the susceptibility could be equally well de-
scribed by simple power-law fits and fits, which use expo-
nents fixed at $3d_{xy}$ values and corrections-to-scaling terms
fixed at the values taken from the heat capacity data and
theory of correction amplitude ratios. In our data analysis we
only used simple power laws to describe the critical diver-
gence of $\xi_\parallel^2$ and, hence, $\xi_\perp^2$ and $\sigma_o$. It would be inter-
esting to see if the analysis from Ref. [17] holds for the
DnAOB mixtures. It would also be interesting to check the
validity of the hyperscaling $\nu_\parallel + 2\nu_\perp = 2 - \alpha$, which appears to be violated if the heat capacity data would show the $3d_{xy}$ value of $\alpha$.

The critical divergence of the correlation lengths and sus-
ceptibility in the 8CB sample was studied only at a 5 T field.
The fits without the mosaicity correction are presented in
Fig. 12, where the average $T_{NA}^{\text{fit}}$ was 0.8 mK less than $T_{NA}^{\text{exp}}$.
The temperature dependences of $\xi_\parallel^2$ and $\sigma_o$ were fit to
single power laws to calculate the critical exponents $\nu_\parallel$

FIG. 12. Log-log plots of $g_\parallel \xi_\parallel^2$ and $\sigma_o$ vs reduced temperature $t$ for 8CB in a 5 T field without a mosaicity correction ($g_\parallel = 0.198 \text{ Å}^{-1}$). The solid lines are the single power-law fits with the exponents given in the text.

FIG. 13. The transverse in-plane $q_\perp$ scan for D6.15AOB in a 5 T field at $t = 9 \times 10^{-6}$. The fits to the structure factor Eq. (2) con-
volved with the appropriate resolution function are shown both
with the fourth order coefficient $c$ being a fitting parameter ($c \neq 0$) and with $c$ being fixed at zero. It is clear that the $c \neq 0$ fit gives
a more adequate description of the experimental profile.

FIG. 14. The fourth order coefficient $c$ for D6.15AOB vs re-
duced temperature $t$ at different fields.
experiments before being strongly affected by mosaicity. If Dasgupta’s argument were to be a good test of this assumption. If Dasgupta’s argument were to hold, there should be a significant decrease in the values of $c$ with increasing field. However, our studies of the three samples under 5 T field indicated that the $c \xi_0^4 q_0^4$ correction term was necessary to obtain acceptable fits (see Fig. 13). Moreover, the high- and low-field values of the coefficient $c$ were essentially the same (see Fig. 14) ruling out any significant effects of mosaicity on the x-ray scattering profile.

VI. CONCLUSION

The critical exponents $\gamma$ and $\nu_{\parallel\perp}$ for the NA transition were measured under a strong (5 T) field in materials with both wide and narrow nematic ranges. The effective transverse resolution in a 5 T field was almost two orders of magnitude better than at low fields and was essentially the instrumental resolution. We have shown that use of a 5 T field would allow one to access three more decades of reduced temperature (up to $t \sim 10^{-8}$) compared to low-field experiments before being strongly affected by mosaicity (but the oven stability sets a considerably higher limit on $t$). The high-field results were not affected by the mosaicity, while the effect of mosaicity on the low-field data for the D6.15AOB sample was clearly observed. The proper Gaussian mosaicity correction was found to be temperature independent but significantly (~3.5 times) smaller than the width of the sharpest $q_0$-scan. No significant effects of mosaicity on the values of the fourth-order coefficient $c$ were observed. The values of the critical exponents obtained from high- and low-field experiments were the same indicating no high-field quenching of the director fluctuations. For all samples the divergence of $\xi_{\parallel\perp}$ and $\sigma$, over the whole range (~4 decades) of reduced temperature were fit well by single power laws. Thus, our data did not exhibit any evidence of a crossover to the strongly anisotropic regime ($\nu_{\parallel}=2\nu_\perp$) for $t<10^{-5}$. The values of the critical exponents for D6.15AOB and D6.4AOB were found, within experimental uncertainties, to be the same indicating that different materials with the NA transitions far from the tricritical point may have the same exponents.

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